

Theorem 2 in Section 1.2

Given any statement variables p , q , and r , a tautology \mathbf{t} and a contradiction \mathbf{c} , the following logical equivalences hold.

- a. *Commutative laws:* $p \wedge q \equiv q \wedge p$ $p \vee q \equiv q \vee p$
- b. *Associative laws:* $(p \wedge q) \wedge r \equiv p \wedge (q \wedge r)$ $(p \vee q) \vee r \equiv p \vee (q \vee r)$
- c. *Distributive laws:* $p \wedge (q \vee r) \equiv (p \wedge q) \vee (p \wedge r)$ $p \vee (q \wedge r) \equiv (p \vee q) \wedge (p \vee r)$
- d. *Identity laws:* $p \wedge \mathbf{t} \equiv p$ $p \vee \mathbf{c} \equiv p$
- e. *Negation laws:* $p \vee \neg p \equiv \mathbf{t}$ $p \wedge \neg p \equiv \mathbf{c}$
- f. *Double negative law:* $\neg(\neg p) \equiv p$
- g. *Idempotent laws:* $p \wedge p \equiv p$ $p \vee p \equiv p$
- h. *De Morgan's laws:* $\neg(p \wedge q) \equiv \neg p \vee \neg q$ $\neg(p \vee q) \equiv \neg p \wedge \neg q$
- i. *Universal bound:* $p \vee \mathbf{t} \equiv \mathbf{t}$ $p \wedge \mathbf{c} \equiv \mathbf{c}$
- j. *Absorption:* $p \vee (p \wedge q) \equiv p$ $p \wedge (p \vee q) \equiv p$
- k. *Negations of \mathbf{t} and \mathbf{c} :* $\neg \mathbf{t} \equiv \mathbf{c}$ $\neg \mathbf{c} \equiv \mathbf{t}$