Autocorrelation, Return Horizons, and Momentum in Stock Returns*

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Abstract

In this study we examine Lewellen's (2002) claim that momentum in stock returns is not due to positive autocorrelation as behavioral models suggest. Using portfolio-specific data, we find that the 6-month/6-month and 12-month/12-month momentum strategies are profitable for the industry, size, and B/M portfolios. Like Lewellen, we find the autocovariance component of the momentum profit to be negative, suggesting no return continuations. However, we also find that the autocorrelations calculated from short-term (e.g., monthly) returns are quite different from long-horizon (e.g., annual) autocorrelations. While the first-order autocorrelations of 6- and 12-month returns tend to be negative, the autocorrelations across twelve lags in monthly returns of the industry, size, and B/M portfolios are in general positive. Our results show that these portfolios exhibit return continuations when returns are measured on a monthly basis. Therefore, our finding appears to be consistent with the behavioral models, which suggest positive autocorrelation in stock returns.

I. Introduction

Among stock return anomalies documented in the finance literature, the profitability of momentum strategies that buy past three- to twelve-month winners and short sell past losers (Jegadeesh and Titman (1993)) remains as a puzzle. Jegadeesh and Titman (2001) document that the profitability of momentum strategies continues in the 1990s, suggesting that their original finding is free of data snooping bias. While momentum strategies tend to generate frequent transactions, Korajczyk and Sadka (2004) find that they remain profitable after accounting for various measures of transaction costs.¹

Several explanations have been proposed to interpret the momentum in stock returns. For instance, Conrad and Kaul (1998) claim that momentum profits are primarily due to cross-sectional variation in unconditional mean returns. According to Conrad and Kaul's arguments (also see Berk, Green, and Naik (1999)), if realized returns are strongly correlated to expected returns, then past winners (losers) that have higher (lower) returns tend to yield higher (lower) expected returns in the future. Consequently, momentum strategies that buy past winners and short sell past losers will yield positive profits because of the cross-sectional dispersion in unconditional mean returns of stocks. However, Jegadeesh and Titman (2001) suggest that Conrad and Kaul's argument cannot explain the long-term (one- to five-year) return reversal effect documented in the literature. Furthermore, Jegadeesh and Titman (2002) show that Conrad and Kaul's results suffer from small sample biases, and when these biases are corrected for in the tests, the variation in mean returns explains very little of the momentum profits.

Another plausible explanation is that abnormal returns from trading strategies are compensations for risk. However, Fama and French (1996) document that while the Fama and French three-factor model can capture most return anomalies, it cannot explain the short-term momentum. Grundy and Martin (2001) provide further evidence showing that the profitability to momentum strategies cannot be

¹ Lesmond, Schill, and Zhou (2004) however suggest that momentum profits reported in prior studies are illusory because of the underestimation of transaction costs. Specifically, they find that momentum strategies require frequent trading in disproportionately loser stocks that tend to be illiquid and hence have larger trading costs. Using various trading cost estimates, they find that costs of executing momentum strategies are much higher than those reported in prior studies, showing that momentum profits are bounded by transaction costs.

explained by exposures to the Fama-French three factors as well as to industry factors. They attribute the major source of the momentum phenomenon to momentum in firm-specified returns.²

Momentum can also be attributed to return continuations. Several existing behavioral models (e.g., Barberis, Shleifer, and Vishny (1998), Daniel, Hirshleifer, and Subrahmanyam (1998), and Hong and Stein (1999)) provide a theoretical framework to explain the empirical return anomalies documented in the finance literature. Despite the differences in their underlying assumptions regarding investors' behavioral biases, these behavioral models all suggest that the momentum effect is closely related to positive autocorrelations in stock returns at short horizons. Daniel et al. suggest that investors might not be rational when making decisions based on available information. They suggest that investors suffer from overconfidence that leads them to overweight private information signals and underweight public information signals. They argue that investor's overconfindence, together with biased self-attribution will produce a pattern of stock price changes that exhibits positive (negative) autocorrelation in the short (long) run. Hong and Stein propose that short-term price momentum is a result of underreaction to information when information diffuses gradually across news watchers. They further argue that the initial underreaction will induce trading from momentum traders and hence in the long run prices will reverse to fundamentals when more and more momentum traders enter the market to earn a profit. Similar to Hong and Stein, Barberis et al.'s model is also based on a short-run underreaction. However, unlike Hong and Stien, they obtain the underreaction by assuming that investors exhibit a conservatism bias, meaning that investors are conservative in updating their priors. In short, according to these behavioral models, price momentum is analogical to positive autocorrelation in stock returns, which could arise because of investors' underreaction or continuing overreaction to news.

 $^{^2}$ Chordia and Shivakumar (2002) however show that profits to momentum strategies are explained by a set of lagged macroeconomic variables and that firm-specific information explains little of the profits. They suggest the predictability of the set of macroeconomic variables on future stock returns arises because these variables capture time-varying returns. Consequently, they argue that their finding is consistent with the argument of Berk, Green, and Naik (1999) that profitability of momentum strategies represents rewards of bearing risk. However, it is noteworthy that simulation based on the model developed by Berk et al. shows that momentum strategy is not profitable for horizons less than 9 months (e.g., 3- and 6-month), which is inconsistent with the empirical finance

Finally, profits to momentum strategies can arise because of cross-sectional correlations among stocks (Lo and MacKinlay (1990)). Lo and MacKinlay show that momentum profits are negatively related to cross-serial correlations, meaning that negative (positive) cross-serial correlations can lead to profits (losses) for a trading strategy that buys winner stocks and short sells loser stocks. Under this scenario, if winner stocks are negatively cross-serially correlated with loser stocks, then a strategy that buys past winners and short sells past losers can generate profits.

Among these possible sources of momentum profits, the results reported by Lewellen (2002) suggest that momentum is mainly driven by cross-serial covariances in stock returns. Lewellen finds that industry, size, and book-to-market portfolios exhibit similar momentum in returns as that for individual stocks. Using the Lo and MacKinlay (1990) method, Lewellen decomposes the portfolio-based momentum profits into three components: (1) negative of the average first-order cross-serial covariance of annual returns of these portfolios, (2) the average first-order autocovariance in annual returns, and (3) the cross-sectional variation of the mean returns of the portfolios. He finds that both the autocovariances and cross-serial covariances are negative, but the latter is more negative than the former. Thus, he concludes that the profitability of portfolio-based momentum strategies is mainly due to cross-serial correlations among portfolio returns. Lewellen argues that his finding of negative autocovariances is inconsistent with the behavioral models, which imply that stock returns are positively serially correlated.

In this study, we attempt to reconcile the apparently conflicting results between the negative autocorrelations as documented in Lewellen (2002) and the analogy between momentum and positive autocorrelation as suggested by existing behavioral models. While the behavioral models do not provide any guidance about the time length of return horizons that will exhibit positive autocorrelation, Lewellen focuses his analysis on annual horizon. We show that the inconsistency between Lewellen's finding and the behavioral models is due to how one measures the length of return horizons. Conceptually, price momentum should be corresponding to positive autocorrelation. Empirically speaking, the existence of

literature. Thus, under Berk et al.'s framework, it is unclear how well rational asset-pricing models can explain the momentum.

momentum could go along with negative autocorrelation because the value as well as the sign of serial correlation could vary with return intervals. In other words, autocorrelations may change sign when returns are measured in different horizons. For instance, consider the S&P 500 total return index (including dividends reinvestments) for the 1941-1999 period—the sample period that we analyze in this study. The first-order autocorrelation is 0.020 for the monthly returns, while it is –0.100 for the annual returns. Moreover, the average of the first twelve-order autocorrelations in the S&P 500 monthly returns is a positive number of 0.004. This finding suggests that the negative autocovariances that Lewellen finds in annual returns could be totally consistent with price momentum, which should be considered more of a phenomenon when pricing adjustments are better evaluated at short, rather than long, intervals. Although the behavioral models do not specify the length of return interval in measuring how stock prices adjust to news, it would be reasonable to expect that the market under- or overreacts to information at a horizon that is much shorter than one year.

To evaluate this issue, we follow Lewellen (2002) and apply the Lo and MacKinlay (1990) momentum decomposition method to industry, size, and book-to-market portfolios for the 1941-1999 sample period. We formulate the portfolio-specific momentum strategies with two intervals, 6 and 12 months. Consistent with Lewellen, we find that both the auto- and cross-serial covariance components of the momentum profit are negative and in general the cross-serial covariances are more negative. As Lewellen indicates, this result implies that momentum is caused by cross-serial covariances, not by positive autocorrelation. However, when the autocorrelations are calculated on monthly returns, most of them are positive. Furthermore, the averages and the cumulative sums of the first six- and twelve-order autocorrelations are mostly positive. Thus, the negative autocovariances associated with momentum as documented in Lewellen and the current study are indeed consistent with the explanation of positive return autocorrelations offered by the behavioral theories. Our results appear to suggest that the relation between price momentum and return autocorrelations is better to be measured by looking at autocorrelations of short-term over various lags rather than autocorrelations of long-term returns. The rest of the paper is organized as follows. Section II describes the momentum strategies that we follow in formulating trading rules and discusses the decompositions of momentum profits into various sources. Section III describes the data, presents the portfolio-based momentum profits and the components of the profits, and analyzes the auto- and cross-serial covariances for those portfolios for various return horizons. The conclusion is in the final section.

II. Momentum Strategies and Sources of Profits

In this paper, we formulate momentum strategies in the same manner as did in Lewellen (2002). Specifically, we consider a strategy that buys or sells stocks at time *t*, based on their performance at time *t* – 1, with *k* horizons between time t - 1 and t.³ The momentum portfolio is constructed with investment weights in stock *i* determined as:

$$w_{i,t-1}(k) = (1/N)[R_{i,t-1}(k) - R_{m,t-1}(k)],$$
(1)

where *N* is the number of stocks available, $R_{i,t-1}(k)$ is the return for stock *i* at time *t* - 1, and $R_{m,t-1}(k) = (1/N) \sum_{i=1}^{N} R_{i,t-1}(k)$ is the return for an equal-weighted portfolio of stock index at time *t* - 1, and *k* is the return interval between time *t* - 1 and *t*. Equation (1) shows that the investment weights are determined based on the performance of stocks against the average return of all stocks. That is, the momentum strategy will buy winner stocks and sell loser stocks at time *t* - 1 and hold the positions at time *t* for a horizon of *k*. By construction, the investment weights lead to a zero-cost, arbitrage portfolio since weights sum to zero, i.e., $\sum_{i=1}^{N} w_{i,t-1}(k) = 0$. Furthermore, bigger winners and losers will receive greater weights, as can be seen clearly from Equation (1).

The profit from this momentum strategy at time t, $\pi_t(k)$, is

$$\pi_t(k) = \sum_{i=1}^N w_{i,t-1}(k) R_{i,t}(k)$$

³ This trading strategy is originally proposed by Lo and MacKinlay (1990) and is employed by Conrad and Kaul (1998) and Jegadeesh and Titman (2002), among others.

$$= \frac{1}{N} \sum_{i=1}^{N} [R_{i,t-1}(k) - R_{m,t-1}(k)] R_{i,t}(k)$$

$$= \frac{1}{N} \sum_{i=1}^{N} [R_{i,t-1}(k) R_{i,t}(k)] - R_{m,t-1}(k) R_{m,t}(k).$$
(2)

Following Lo and MacKinlay (1990) and assuming that unconditional mean returns of individual stocks are constant, we can decompose the momentum profit into various components by taking expectations of Equation (2):

$$E[\pi_{t}(k)] = \frac{1}{N} \sum_{i=1}^{N} E[R_{i,t-1}(k)R_{i,t}(k)] - E[R_{m,t-1}(k)R_{m,t}(k)]$$

$$= \frac{1}{N} \sum_{i=1}^{N} (Cov[R_{i,t-1}(k), R_{i,t}(k)] + \mu_{i}^{2}(k)) - (Cov[R_{m,t-1}(k), R_{m,t}(k)] + \mu_{m}^{2}(k))$$

$$= -Cov[R_{m,t-1}(k), R_{m,t}(k)] + \frac{1}{N} \sum_{i=1}^{N} Cov[R_{i,t-1}(k), R_{i,t}(k)]$$

$$+ \frac{1}{N} \sum_{i=1}^{N} [\mu_{i}(k) - \mu_{m}(k)]^{2}$$
(3)

Equation (3) indicates that the expected profits of momentum strategies come from three sources: (1) the negative of the first-order autocovariance of the k-period returns for the equal-weighted market portfolio, (2) the average of the first-order autocovariances of the k-period returns of the N stocks, and (3) the variance of the mean returns of the N stocks. Note that if all stock prices follow random walks and hence all the first-order autocovariances equal zero, then the expected momentum profit equals to the cross-sectional variation in mean returns. This is what Conrad and Kaul (1998) find, in which they document that momentum is attributable to cross-sectional dispersion in mean returns, not to time-series predictability in returns.

Also note that if we assume every stock has the same mean return, it is easy to see that price momentum (i.e., positive autocovariance) does not necessarily lead to momentum profit. When individual stocks exhibit positive autocovariance, it is reasonable to expect that the equal-weighted market portfolio will also show positive autocovariance. Therefore, in the absence of cross-sectional variation in mean returns, whether a momentum strategy is profitable or not would depend on the relative magnitudes between the autocovariances of the market portfolio and those of the individual stocks. Moreover, as Atchison, Butler, and Simonds (1987) demonstrate, the autocorrelation of a well-diversified portfolio is approximately equal to the average cross-serial covariance between the stocks divided by the average contemporaneous covariance between these stocks. Accordingly, cross-serial covariances between stocks also affect momentum profits.

To see how momentum is affected by cross-serial covariances between individual stocks as well as by autocovariances, note that Equation (3) can be rewritten as follows:

$$E[\pi_{t}(k)] = -\{Cov[R_{m,t-1}(k), R_{m,t}(k)] - \frac{1}{N^{2}} \sum_{i=1}^{N} Cov[R_{i,t-1}(k), R_{i,t}(k)]\} + \frac{N-1}{N^{2}} \sum_{i=1}^{N} Cov[R_{i,t-1}(k), R_{i,t}(k)] + \frac{1}{N} \sum_{i=1}^{N} [\mu_{i}(k) - \mu_{m}(k)]^{2} = -C_{1} + O_{1} + \sigma^{2}(\mu).$$

$$(4)$$

Equation (4) shows that the profitability of a momentum strategy depends not only on the first-order autocovariances of individual stocks, denoted by O_1 , but also on the first-order cross-serial covariances, denoted by C_1 . Momentum profits can also be due to the cross-sectional variation in mean returns of the N stocks, $\sigma^2(\mu)$. In summary, the decomposition shows that momentum profits result form three sources. First, stock returns are negatively cross-serially correlated, implying that a stock with a high return today is associated with low returns in the future for other stocks. Second, individual stocks might be positively serially correlated, implying that a stock with a high return today is expected to have high returns in the future. The final source arises because momentum strategy tends to buy stocks with a high mean return and short sell others with a low mean return. The results reported by Lewellen (2002) seem to support the view that momentum is driven by cross-serial covariances between stock returns. Lewellen finds that momentum strategies applied on industry, size, and book-to-market portfolios exhibit similar profits as those for individual stocks. He also finds that the portfolio-based momentum is mainly due to cross-serial covariances between these portfolios because both the average auto- and cross-serial covariances are

negative, but the latter is more negative than the former. Apparently, Lewellen's finding is inconsistent with the behavioral models, which imply that stock returns are positively serially correlated. Lewellen hypothesizes that the negative cross-serial covariances are a result from the combination of investors' underreactions to firm-specific news and overreactions to macroeconomic news.

Alternatively, Conrad and Kaul (1998) assert that momentum profits are mainly driven by the variation in the mean returns of individual equities, not by the time-series predictability in stock returns. They interpret momentum as variations in risk across assets. Intuitively, if realized returns are strongly correlated to expected returns, then momentum strategies that buy past winners and short sell past losers will yield positive profits because winners (losers) that have higher (lower) realized returns tend to yield higher (lower) expected returns in the future. To see this, consider the case that stock returns are both serially and cross-sectionally uncorrelated (i.e., stock returns are not predictable), then both the first and the second terms in Equation (4) become zero and hence the entire momentum profit is due to the cross-sectional variation in mean returns. Thus, in the absence of predictability in stock returns, momentum can still arise as long as there are significant variations in mean returns or time-varying risk premiums. Nevertheless, Jegadeesh and Titman (2002) provide results showing that Conrad and Kaul's results suffer from small sample biases, and when these biases are corrected for in the tests, the variation in mean returns explains very little of the momentum profits.⁴

III. Data, Momentum Profits, and Autocorrelations

A. Data

For the purpose of comparison with Lewellen (2002), we conduct our analyses on portfolios, instead of individual stocks. Monthly return data for industry, size, and book-to-market (B/M) portfolios

⁴ Since both Conrad and Kaul and Jegadeesh and Titman focus on the contribution of the cross-sectional variation of mean returns to momentum profits, they combine the auto- and cross-serial covariance terms into a time-serial predictability term. Kaul and Jegaseesh's result indeed implies that momentum effect is mainly due to time series predictability in stock returns.

are retrieved from Kenneth French's website.⁵ We examine the period 1941-1999 because Lewellen considers this sample period. These portfolio return data are compiled using all NYSE, AMEX, and Nasdaq common stocks. We use the 12 industry portfolios and 10 size and B/M decile portfolios. Stocks are grouped into industries according to their four-digit SIC codes at the end of June of each year. Size portfolios are constructed using the market equity value at the end of each June and using NYSE breakpoints. B/M portfolios are based on the book-to-market ratio at the end of previous fiscal year. The breakpoints for the B/M portfolios are based on those stocks that have data on book value. We conduct the analysis on both value- and equal-weighted portfolios, but only report the results for the value-weighted portfolios are qualitatively the same.

B. Profits to momentum strategies

Lewellen (2002) form momentum portfolios based on past 6- and 12-month returns and calculate momentum profits each month up to 18 months after formation. Since our objective is to evaluate the relation between autocovariances and return horizons, we perform the analysis with a ranking period equals to the evaluation period. Table 1 reports the profits to momentum strategies implemented on the different sets of portfolios for two different horizons, with *k* equals 6 and 12 months. The portfolio-based momentum strategies are profitable except for a 6-month strategy implemented on the B/M portfolios. Indeed, the 6-month strategy applied to the B/M portfolios yields a loss, which is somewhat surprising given the finding of Chan, Jegadeesh, and Lakonishok (1996). Chan et al. find that past 6-month winners tend to be glamour stocks with low book-to-market ratios, while past 6-month losers tend to be value stocks with high book-to-market ratios. The *z*-statistics,⁶ which are asymptotically standard normal under the null hypothesis that the "true" profits are zero, show that only the 12-month momentum strategy applied to the industry and size portfolios generates statistically significant profits.

⁵ The website's address is http://mba.tuck.dartmouth.edu/pages/faculty/ken.french/data_library.html.

 $^{^{6}}$ The *z*-statistics are corrected for heteroskedasticity and autocorrelations up to eight lags based on the adjustments outlined in Newey and West (1987).

Given our small sample size (59 for the 12-month analysis), the statistical power of the asymptotic statistics tends to be low. To remedy this problem, we perform a bootstrap test. For the bootstrap test, we shuffle (without replacement) the sets of monthly portfolio returns simultaneously so that both auto- and cross-serial correlations in the data are eliminated.⁷ A total of 1,000 replications are implemented. The results from the bootstrap analysis are also provided in Table 1. We focus on using the *p*-value, which is the probability that the 1,000 bootstrap profits are less (larger) than the sample average profit if the sample value is less (larger) than the median of the bootstrap distribution, for statistical inference. The statistical inferences based on the bootstrap analysis are very similar to those from the asymptotic *z*-statistics. Again, the bootstrap *p*-value suggests that the 12-month momentum strategy applied to the industry and size portfolios yields statistically significant profits at the 5 percent level.

Table 1 also reports the momentum profit components based on Equation (4). Consistent with Lewellen (2002), we find the auto- and cross-serial covariances are both negative, except the autocovariance term from the 12-month strategy applied on the size portfolios. Moreover, the cross-serial covariances are in general more negative than the autocovariances. Since momentum profit is contributed by autocovariance positively but by cross-serial covariance negatively, the more negative cross-serial covariance value along with negative autocovariance means that return continuations may not be the source of the momentum profits. Rather, cross-serial covariance appears to dominate the momentum, even though for most of the cases its contribution is partially offset by the autocovariance component. Nevertheless, none of the auto- and cross-serial covariance components is significant at any conventional level based on either asymptotic *z*-statistics or bootstrap estimates.

The cross-sectional variation in the mean returns of these portfolios appears not to affect the momentum significantly for the industry and size portfolios. However, the dispersion in mean returns of

⁷ Usually bootstrap experiments are done with replacement (e.g., see Conrad and Kaul (1998)). However, as Jegadeesh and Titman (2002) show, bootstrap experiments where returns are drawn with replacement will overestimate the cross-sectional variation in stock mean returns for small samples. Thus, even though shuffling has eliminated any time- and cross-serial dependence in stock returns, bootstrapping with replacement may still generate

the B/M portfolios seems to be an important component compared to the time-series predictability because the sum of the auto- and cross-serial covariance components is negative (the 6-month horizon) or one component is almost entirely offset by the other (the 12-month horizon). Similar results have also been documented in Conrad and Kaul (1998), in which they emphasize whether profits to trading strategies are from the time-series predictability in returns (i.e., sum of $-C_1$ and O_1) or from the variation in mean returns. Since the two time-series predictability components may offset each other, combining them together in the analysis might overestimate the importance of the variance of mean returns to the profits of momentum strategies.

C. Auto- and cross-serial correlations

As Table 1 shows, the averages of the first-order auto- and cross-serial covariance in 6- and 12month returns of the industry, size, and B/M portfolios are in general negative. To explore how these portfolios' returns are correlated with their own returns and other portfolios', we calculate the first-order auto- and cross-serial correlations in semi-annual and annual returns. Tables 2, 3, and 4 report the estimates for the industry, size, B/M portfolios, respectively. As can be seen, these portfolios' returns not only negatively correlated with their past returns but also negatively cross-serially correlated with other portfolios' returns. Most of the portfolios' first-order autocorrelations (the entries in diagonals) are negative. For the industry and B/M portfolios, the average of the first-order autocorrelations (the last diagonal item) becomes more negative when the horizon increases from 6 months to 12 months, but this is not the case for the size portfolios.

Apparently, these cross-serial correlation matrices are not symmetric. For the size and B/M portfolios, elements below the diagonal are greater than those above it, indicating a lead-lag relation between these portfolios. Specifically, large stocks appear to lead those of smaller stocks, and high B/M stocks lead lower B/M stocks. Unlike the size and B/M portfolios, the industry portfolios do not exhibit

significant profit because of the small sample bias.

such lead-lag relations. Consistent with the momentum profit decomposition results reported in Table 1, most the averages of these cross-serial covariances are negative.

As can be seen in Table 2, the first-order cross-serial correlations in returns of the industry portfolios tend to be larger (in absolute value) than the autocorrelations. For instance, at a 6-month horizon, the average of the cross-serial correlations is -0.036 (calculated from the twenty-four average cross-serial correlation figures in Table 2), which is much smaller than that of the autocorrelations (i.e., -0.003). Similar results also hold for the size portfolios (see Table 3). This finding of larger (in absolute value) cross-serial correlations is consistent with Table 1, as well as with Lewellen's (2002) claim that the main contribution to the momentum profit comes from negative cross-serial correlations between securities. The B/M portfolios, however, do not show that the cross-serial covariance dominates the momentum. The average of the semi-annual cross-serial correlations (-0.024, calculated from the twenty average figures in Table 4) of the B/M portfolios is slightly larger than the semi-annual autocorrelation (-0.027), whereas the average annual cross-serial correlation (-0.082).

D. Autocorrelations and the return horizon

The evidence presented so far supports the idea that negative cross-serial correlations between securities are the driving force of the intermediate-horizon momentum. Return continuations (positive autocorrelations), as behavioral models (e.g., Barberis et al. (1998), Daniel et al. (1998), and Hong and Stein (1999)) suggest, cannot explain the momentum because negative return autocorrelations are found at intermediate horizons, such as 6- and 12-months. It is noteworthy, however, that short-run momentum (long-term reversals) is associated with positive (negative) autocorrelation of short-term returns separated by short (long) lags. For instance, Hong and Stein's (1999) Proposition 2 indicates that a momentum strategy will be profitable for a horizon k if the cumulative autocovariances of returns up to k - 1 is not zero (p. 2154). According to Hong and Stein, when cumulative autocorrelations of short-horizon returns

are positive up to a certain lag order, price momentum will arise. In other words, return continuations that the behavioral models refer to are a feature that is more to do with short-horizon returns than with longhorizon returns. On the other hand, the Lo and MacKinlay (1990) decomposition method allows us to evaluate only the first-order autocorrelation of long-horizon returns, not the autocorrelations of short-term returns separated by short lags. Therefore, one possible explanation that the momentum decomposition result does not show return continuations as predicted by the behavioral models is due to its failure of capturing the autocorrelations of short-horizon returns. Moreover, intuitively it seems to be more appropriate to rely on short-horizon returns, rather than long-horizon returns, if one wants to measures investors' over- or underreaction to information arriving to the market. In short, our view is that, even though long-horizon stock returns are negatively serially correlated, short-horizon stock returns could show positive autocorrelations.

To investigate this possibility, we calculate autocorrelations of monthly returns for first order to twelfth order. Table 5 provides estimates of these monthly autocorrelations. Most autocorrelations are positive and not significantly different from zero, except for the first-order autocorrelations. Unlike annual autocorrelations, all the first-order monthly autocorrelations are positive, suggesting that return continuations do exist. However, after a price continuation for two consecutive months, stock prices in general take a correction at the opposite direction in the following month, as negative second-order autocorrelations imply. Consistent with the literature, small-firm portfolios display larger first-order autocorrelations than those of large-firm portfolios. The larger autocorrelations for small-firm portfolios likely are induced by much slow pricing adjustments to information by small firms compared to larger firms.⁸

To get a clear picture of autocorrelation patterns, we calculate the average of the autocorrelations for lags 1-6 and 1-12 separately as well as their cumulative sum. The average autocorrelation and the cumulative autocorrelation over 6 months are uniformly positive for the industry, size, and B/M

⁸ Hong, Lim, and Stein (2000) find that momentum strategies become less profitable when extreme small stocks are excluded from the analysis. Their finding suggests that small stocks exhibit more pronounced momentum and

portfolios. Similar to the first-order autocorrelation, the average and the cumulative autocorrelations over 6 months decline as firm sizes increase. The majority of the average and the cumulative autocorrelation over 12 months are also positive. Overall, the results in Table 5 indicate that autocorrelations across 12 months are in general positive. Consequently, our findings support the behavioral models' argument that momentum is analogous to positive medium-term autocorrelations in stock returns.

IV. Conclusions

In this study we examine Lewellen's (2002) claim that momentum is not due to positive autocorrelation as suggested by existing behavioral modes. All the behavioral models have corresponded momentum with positive autocorrelation. Using portfolio-specific data, we find that the 6-month/6-month and 12-month/12-month momentum strategies are profitable for the industry, size, and B/M portfolios. Consistent with Lewellen, we find that the autocovariance components of the momentum profits are in general negative. This finding appears not to support the correspondence between momentum and positive autocorrelations in stock returns. The autocorrelation analysis also shows that both the first-order auto- and cross-serial correlations in 6- and 12-month portfolio returns are negative.

We argue that the analogous between positive autocorrelation and momentum is better evaluated by using short-term returns. That is, momentum arises because short-horizon returns are positively serially correlated over short lags. The monthly autocorrelations seem to support this conjecture. Specifically, most autocorrelations across twelve lags in monthly returns of the industry, size, and B/M portfolios are positive. Our results therefore imply that these portfolios exhibit return continuations, which appear to be consistent with the behavioral models.

positive autocorrelations because they adjust more slowly to news than larger stocks.

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Table 1 Profits to Momentum Strategies and Auto- and Cross-serial Covariances

This table contains the decomposition of average profits of momentum strategies that long past winner portfolios and short past loser portfolios for the period 1941-1999. Expected profit is given by $E[\pi_t(k)] = -C_1 + O_1 + \sigma^2(\mu)$, where C_1 mainly depends on the average first-order cross-serial covariance of the portfolio returns, O_1 depends on the average first-order autocovariance, and $\sigma^2(\mu)$ is the cross-sectional variance of the mean returns. The numbers in parentheses are z-statistics that are asymptotically N(0,1) under the null hypothesis that the relevant parameter is zero, and are robust to autocorrelation and heteroskedasticity. The p-value reports the probability that the 1,000 bootstrap average profits from the bootstrap distribution are less (larger) than the sample average profit if the sample value is less (larger) than the median of the bootstrap average profits from the bootstrap distribution are less (larger) than the sample average profit if the sample value is less (larger) than the function bootstrap average profits from the bootstrap distribution are less (larger) than the sample average profit if the sample value is less (larger) than the function bootstrap average profit if the sample value is less (larger) than the bootstrap distribution. The p-value reports the probability that the 1,000 bootstrap average profit if the sample value is less (larger) than the median of the bootstrap distribution. All profit estimates are multiplied by 1,000.

Horizon	$E[\pi_t(k)]$	C_1	01	$\sigma^2(\mu)$
12 industry va	lue-weighted portfol	ios		
6-month	0.375	-0.564	-0.218	0.029
	(1.41)	(-0.42)	(-0.14)	
	p = .011	p = .333	p = .473	
12-month	1.027	-1.485	-0.574	0.116
	(1.86)	(-0.48)	(-0.17)	
	p = .024	<i>p</i> = .336	p = .500	
10 size value-	weighted portfolios			
6-month	0.068	-0.698	-0.648	0.017
	(0.50)	(-0.36)	(-0.33)	
	p = .333	p = .384	p = .403	
12-month	1.553	-0.739	0.745	0.069
	(2.29)	(-0.14)	(0.13)	
	p = .001	p = .471	p = .402	
10 B/M value-w	eighted portfolios			
6-month	-0.028	-0.279	-0.396	0.089
	(-0.24)	(-0.20)	(-0.28)	
	p = .219	p = .450	p = .421	
12-month	0.540	-1.829	-1.644	0.354
	(1.07)	(-0.49)	(-0.40)	
	p = .229	p = .319	$\varphi = .355$	

Table 2Autocorrelations and Cross-serial Correlations of Industry Portfolios

This table reports first-order autocorrelations (diagonals) and cross-serial correlations (off diagonals) for lag 1 of the returns of 12 industry portfolios. The industry portfolios are constructed based on four-digit SIC codes. Ind1 is for consumer non-durables, Ind2 is for consumer durables, Ind3 is for manufacturing, Ind4 is for energy, Ind5 is for chemicals, Ind6 is for business equipment, Ind7 is for telecommunication, Ind8 is for utilities, Ind9 is for wholesale and retail, Ind10 is for healthcare, Ind11 is for finance, and Ind12 is for all other industries. The entry in the *i*th row and *j*th column is the correlation between $R_{i,t-1}$ and $R_{j,t}$. Standard error is calculated as $1/\sqrt{T}$, where T is the number of non-overlapping returns. T is 118 for semi-annual returns, and is 59 for annual returns. Bold denotes estimates are significantly different from zero at the 10% level.

Portfolio	Indl	Ind2	Ind3	Ind4	Ind5	Ind6	Ind7	Ind8	Ind9	Ind10	Ind11	Ind12	Average
Semi-annual	returns												
Ind1	000	060	057	073	031	105	.079	.044	032	008	052	069	033
Ind2	085	042	032	069	019	.004	.078	.001	051	034	094	025	030
Ind3	120	098	065	079	049	082	027	081	115	044	148	104	086
Ind4	044	.018	.028	015	.050	006	079	093	.000	003	087	003	020
Ind5	126	069	079	077	042	111	027	069	111	063	160	134	093
Ind6	095	079	037	115	079	021	.016	078	086	065	076	064	069
Ind7	041	.039	028	066	009	.026	.196	.014	.027	021	096	021	016
Ind8	.165	.153	.163	.074	.146	.103	.192	.140	.189	.108	.077	.142	.137
Ind9	114	116	125	160	098	107	.003	025	116	058	132	147	098
Ind10	104	118	092	155	068	109	046	- .067	115	014	150	153	107
Ind11	.024	.050	.008	033	.050	010	.103	.037	.059	.033	007	.002	.029
Ind12	063	036	042	090	002	044	.010	027	044	021	103	050	042
Average	055	029	027	077	010	040	.027	031	025	016	093	052	003
Annual retur	ns												
Indl	.037	031	.013	.039	.018	086	.113	.047	.019	.065	.049	000	.022
Ind2	178	090	030	.040	076	054	.065	009	135	110	078	072	058
Ind3	201	242	107	.007	149	205	096	090	265	076	112	192	147
Ind4	266	270	211	054	191	263	181	147	297	048	161	185	202
Ind5	165	112	039	.082	036	136	.024	051	194	055	094	126	079
Ind6	108	072	.019	.104	054	.019	.098	.006	084	069	.069	022	010
Ind7	115	005	116	122	041	.021	.069	- .097	043	078	196	144	085
Ind8	029	036	.044	031	.039	032	.018	- .031	020	.007	098	014	014
Ind9	075	.022	.041	.049	003	034	.093	.011	022	028	.016	007	.008
Ind10	079	088	039	.018	025	076	021	108	091	002	113	103	066
Ind11	164	081	078	040	036	101	011	- .055	105	013	068	111	072
Ind12	114	152	042	001	101	113	079	038	141	.000	077	077	078
Average	121	097	040	.013	056	098	.002	048	123	037	072	089	030

Table 3Autocorrelations and Cross-serial Correlations of Size Portfolios

This table reports first-order autocorrelations (diagonals) and cross-serial correlations (off diagonals) for lag 1 of the returns of 10 size-sorted decile portfolios. The entry in the *i*th row and *j*th column is the correlation between $R_{i,t-1}$ and $R_{j,t}$. Standard error is calculated as $1/\sqrt{T}$, where T is the number of non-overlapping returns. T is 118 for semi-annual returns, and is 59 for annual returns. Bold denotes estimates are significantly different from zero at the 10% level.

Portfolio	Small	2	з	4	5	6	7	8	9	Large	lverage
				-			,			Large	
Comi onnuol	maturna										
Sellit-allilual	. ietuins	014	0.25	010	050	0.4.0	054	0.0.2	070	070	0.5.0
Small	015	014	035	018	052	042	054	083	079	0/2	050
2	004	009	039	018	054	049	057	095	086	061	051
3	012	019	056	038	066	063	070	110	095	073	061
4	003	008	045	027	058	054	064	101	086	064	054
5	.009	.001	038	016	048	049	057	092	082	048	041
6	.020	.009	030	010	043	043	052	094	077	045	036
7	.034	.027	014	.008	024	024	031	072	054	012	015
8	.029	.024	021	.001	028	036	039	- .079	064	021	017
9	.029	.031	010	.013	016	016	019	052	032	.022	002
Large	043	038	082	060	080	076	074	- .111	071	012	071
Average	.004	.001	035	015	047	045	054	090	077	042	035
Annual retu	ırns										
Small	.132	.119	.104	.075	.085	.078	.043	.002	.011	043	.053
2	.072	.071	.055	.028	.045	.041	.012	027	019	049	.018
3	.024	.025	.013	011	.007	.006	027	063	054	076	019
4	.010	.021	.005	019	.007	.008	021	054	044	053	013
5	015	.000	012	029	016	005	038	071	065	062	033
6	042	033	041	061	044	034	065	097	087	085	062
7	- 061	- 041	- 053	- 063	- 046	- 038	- 059	- 091	- 077	- 057	- 059
8	- 073	- 054	- 065	- 075	- 059	- 043	- 072	- 103	- 096	- 068	- 067
9	- 095	- 059	- 077	- 083	- 067	- 053	- 059	- 090	- 076	- 022	- 067
Jarge	- 211	- 166	_ 190	- 192	- 156	- 158	- 138	- 155	- 131	- 047	- 166
Juarage	211	100	020	192	130	10	130	133		047	100
Average	026	021	030	046	025	018	041	0/2	062	057	014

Table 4Autocorrelations and Cross-serial Correlations of Book-to-Market Portfolios

This table reports first-order autocorrelations (diagonals) and cross-serial correlations (off diagonals) for lag 1 of the returns of 10 book-to-market decile portfolios. The entry in the *i*th row and *j*th column is the correlation between $R_{i,t-1}$ and $R_{j,t}$. Standard error is calculated as $1/\sqrt{T}$, where T is the number of non-overlapping returns. T is 118 for semi-annual returns, and is 59 for annual returns. Bold denotes estimates are significantly different from zero at the 10% level.

Portfolio	Low	2	3	4	5	б	7	8	9	High	Average
Semi-annual	returns										
Low	081	156	139	132	080	085	072	077	107	089	104
2	045	102	068	067	038	043	043	047	067	063	053
3	.003	058	021	029	004	020	022	009	042	059	027
4	046	087	072	044	033	041	031	014	036	035	044
5	.058	009	.010	.029	.035	.018	.010	.046	.013	005	.019
6	.011	035	015	.008	.016	.009	.009	.034	004	.004	.003
7	.040	006	.006	.037	.019	.028	.015	.036	.005	.003	.019
8	.047	.002	.017	.020	.020	.031	.006	.036	.010	005	.016
9	009	053	024	018	005	020	043	008	038	045	025
High	014	048	032	034	030	031	061	- .038	060	075	039
Average	004	050	035	021	015	018	027	009	032	033	027
Annual retu	ırns										
Low	062	127	150	084	081	063	120	109	122	128	109
2	050	080	101	022	025	011	101	110	086	078	065
3	016	043	069	.010	019	013	092	098	071	102	049
4	059	068	106	034	043	030	080	116	065	073	071
5	034	070	106	018	037	027	082	086	052	069	060
6	117	158	171	103	100	102	147	- .160	127	144	136
7	111	121	146	090	098	080	149	- .154	116	112	114
8	120	154	170	111	064	073	159	- .155	131	139	125
9	056	066	106	049	019	010	090	099	049	048	060
High	134	133	147	085	036	031	119	132	091	080	101
Average	076	104	134	061	054	038	110	118	096	099	082

Table 5 Autocorrelations in Industry, Size, and B/M Portfolios

This table reports autocorrelations (ρ_k) for lags 1-12 of the monthly returns for value-weighted industry, size, and B/M portfolios. Ind1 is for consumer non-durables, Ind2 is for consumer durables, Ind3 is for manufacturing, Ind4 is for energy, Ind5 is for chemicals, Ind6 is for business equipment, Ind7 is for telecommunication, Ind8 is for utilities, Ind9 is for wholesale and retail, Ind10 is for healthcare, Ind11 is for finance, and Ind12 is for all other industries. ρ_{1-6} and ρ_{1-12} are the average autocorrelation for lags of 1-6 and of 1-12, respectively. $\rho_{1-6,s}$ and $\rho_{1-12,s}$ report the cumulative autocorrelation for lags of 1-6 and of 1-12, respectively. Q(k) is the Ljung-Box Q statistic for k order autocorrelation. Bold denotes estimates are significantly different from zero at the 10% level.

Portfolio	$ ho_1$	$ ho_2$	$ ho_3$	$ ho_4$	$ ho_5$	$ ho_{6}$	$ ho_{8}$	$ ho_{10}$	$ ho_{12}$	$ ho_{ t l-6}$	$ ho_{1-12}$	$ ho_{1-6,s}$	$ ho_{ extsf{1-12,s}}$	Q(6)	Q(12)
12 industry value-weighted portfolios															
Indl	.132	015	010	.006	.079	036	003	015	.042	.026	.018	.156	.210	18.74	19.74
Ind2	.083	.028	006	012	.037	040	014	.018	.027	.015	.012	.090	.146	7.75	10.33
Ind3	.083	019	025	017	.020	036	038	018	.001	.001	014	.006	044	7.07	8.43
Ind4	.027	032	.012	.039	.048	034	076	031	.026	.010	001	.060	014	4.91	10.87
Ind5	.027	049	.021	002	.055	035	014	021	.021	.003	.000	.017	.002	5.51	6.47
Ind6	.077	015	.021	012	005	021	024	023	.037	.008	.007	.045	.082	5.17	7.94
Ind7	.052	.003	.087	007	.077	007	.019	.007	.064	.034	.022	.205	.267	11.67	18.01
Ind8	.086	050	.017	.079	.155	015	024	004	.018	.045	.022	.272	.268	29.07	29.84
Ind9	.165	.005	040	025	.044	066	014	.044	.026	.014	.012	.083	.143	25.42	32.25
Ind10	.052	.003	023	.032	.038	054	.032	026	.055	.008	.012	.048	.146	6.15	10.63
Ind11	.123	018	018	.022	.063	011	101	036	.039	.027	.005	.161	.058	14.53	23.88
Ind12	.121	.010	027	008	.032	026	105	014	.014	.017	001	.102	008	12.32	21.06
Average	.086	012	.001	.008	.054	032	030	010	.031	.017	.009	.104	.105		
10 size val	ue-wei	ghted p	ortfoli	os											
Small	.220	001	001	.034	.005	.032	041	032	.122	.048	.028	.289	.339	36.02	50.32
2	.194	.020	014	003	.002	.007	058	031	.070	.034	.019	.206	.227	27.09	34.16
3	.164	010	024	012	004	.002	072	023	.046	.019	.007	.116	.084	19.69	25.89
4	.177	007	026	025	.005	.005	070	030	.033	.022	.009	.129	.105	23.38	28.90
5	.145	005	012	013	.010	002	080	030	.019	.021	.004	.123	.044	15.35	21.42
6	.144	012	023	023	.027	007	094	023	.019	.018	.002	.106	.025	16.08	23.45
7	.130	006	017	006	.034	012	078	021	.001	.021	.002	.123	.021	13.18	18.08
8	.096	005	028	025	.049	027	077	035	.002	.010	008	.060	092	9.84	15.56
9	.083	019	020	.005	.052	031	059	019	.005	.012	004	.070	044	8.05	11.30
Large	.020	014	.014	.017	.093	057	010	021	.054	.012	.007	.073	.082	9.26	11.82
Average	.137	006	015	005	.027	009	064	027	.037	.022	.007	.130	.079		

Table 5-Continued

10 B/M valu	10 B/M value-weighted portfolios														
Low	.094	018	.005	005	.046	047	010	031	.044	.013	.005	.075	.062	9.68	12.02
2	.067	041	022	001	.044	038	068	013	.014	.002	005	.009	061	7.18	10.83
3	.071	044	001	.004	.062	036	063	008	.004	.009	003	.056	037	8.57	12.05
4	.083	034	026	.025	.081	040	067	.017	002	.015	.002	.089	.026	12.42	16.02
5	.064	031	024	.020	.102	010	084	013	.010	.020	.003	.121	.037	11.77	17.09
б	.047	017	.027	.001	.074	027	103	019	.008	.018	.000	.105	.003	6.73	14.64
7	.023	.039	.033	020	.104	034	031	045	.000	.024	.004	.145	.043	11.03	13.39
8	.039	.029	.007	002	.072	.005	079	035	.058	.025	.008	.150	.096	5.38	13.69
9	.080	.002	.018	.007	.038	008	060	054	.058	.023	.007	.137	.078	5.92	13.36
High	.110	.018	042	.006	.011	.010	079	061	.062	.019	.003	.113	.031	10.24	21.30
Average	.068	010	003	.004	.063	023	064	026	.026	.017	.002	.100	.028		