

## Time Series Analysis and Seasonal Decomposition

### Examine Periodicity in the Data

Here we are looking for some evidence that the time series has periodicity... in this case yearly cycles.

#### **Analyze > Forecasting > Sequence Charts...**

Variables: CO2

Time Axis Label: Date

#### **Analyze > Forecasting > Autocorrelations...**

Variables: CO2

Our version of SPSS does not have the correct modules to do seasonal decomposition automatically, so we must do it ourselves.

#### *Steps in Additive Time Series Decomposition*

1. Calculate the trend-cycle component ( $Tt$ ) using moving averages.
2. Calculate a de-trended series by subtracting the trend from the observation ( $yt - Tt$ ).
3. Estimate the seasonal component ( $St$ ) for each period (e.g. month) by averaging the de-trended values for that period.
4. Calculate the remainder (error) component by subtracting both the seasonal and trend-cycle components from the observation ( $Et = yt - St - Tt$ ).

### Step 1: Create Seasonal (Trend Cycle) Component:

#### **Transform > Create Times Series...**

CO2, Center Moving Average

Span=12

Name = CO2\_Trend

Note that centered moving average in SPSS removed observations from both the beginning and the end of the time series.

### Step 2: Create the Detrended Series:

#### **Transform > Compute Variable...**

CO2\_Detrend = CO2 - CO2\_Trend

### Step 3: Estimate the Seasonal Component:

Next you would compute the mean CO2\_Detrend for each month and then copy the mean CO2\_Detrend for each year. I have done this for you...CO2\_Seasonal.

#### **Data > Split File...**

Organize Output Groups by: Mo

**Analyze > Descriptive Statistics > Descriptives**

Variables: CO2\_Detrend

**Data > Sort Cases**

Variables: Date

Then you input for each month the monthly mean CO2\_Detrend for the entire series. Copy and paste works here...

**Step 4: Calculate the Error Component:**

**Transform > Compute Variable...**

CO2\_Error = CO2 – CO2\_Trend – CO2\_Seasonal

**Step 5: Generate Seasonality Plots**

**Analyze > Forecasting > Sequence Charts...**

Variables: CO2, CO2\_Trend

Time Axis Label: Date

**Analyze > Forecasting > Sequence Charts...**

Variables: CO2\_Seasonal, CO2\_Error

Time Axis Label: Date

**Step 5: Determine if the Trend is Significant:**

Create a new variable called **NumDate**.

Open a new syntax window and enter the command below:

**formats NumDate(f1).**

Copy the Date variable into the NumDate variable using **Cut (ctrl V)** and **Paste (ctrl C)**.

Note that the Julian date format has changed into a numeric format. These represent the numbers of seconds between the year 1582 and a given time on a given date, with each year being **3155760** seconds long.

To calculate 1 year in the future, you will need to know the numeric last date in the time series and then use the following equation:

New Date = Numeric Last Date in Time Series + Number of Years into the Future(31557600)

For example: Determine the numeric date of Dec 1987

Dec 1985 = 12721622400

Dec 1987 = 12721622400 + 2(31557600) = 12784737600

Run the regression using NumDate as the independent variable and CO2\_Trend as the dependent variable.

Remember that the regression equation is in terms of the number of seconds.