

***Quantitative Methods***  
***Geography 441***

**Course Requirements**

## **Exercises**

- **Must be handed in on time.**
- **Must be TYPED.**
- **Must follow the format provided. Some slight variation if fine, as long as it is legible.**
- **IF you use Microsoft WORD, get used to working with the EQUATION EDITOR.**

*The formats below are to be used when completing the exercises and tests for this course.*

Format for Hand Calculation:

Research Question: One hundred and fifty students in Geo 441 were surveyed to determine if the use of the correct answer format was associated with student survival.

*Clearly stated  
research question*

$H_o$  : Student survival is independent of using the correct answer format.

*Null and alternate  
hypotheses statements*

$H_A$  : Student survival is contingent upon using the correct answer format.

$\sigma = 0.05$

*Alpha level*

Observed

	Dead	Alive	Total
Used Format	17	54	71
Did Not Use Format	67	12	79
Total	84	66	150

*Clearly typed problem*

Expected

	Dead	Alive
Used Format	39.8	31.2
Did Not Use Format	44.2	34.8

$$\chi^2 = \frac{(17 - 39.8)^2}{39.8} + \frac{(54 - 31.2)^2}{31.2} + \frac{(67 - 44.2)^2}{44.2} + \frac{(12 - 34.8)^2}{34.8} = 56.4$$

*Clearly typed answer*

$$\chi^2 = 56.4$$

$$Df = 1$$

$$\chi^2_{c, 0.05, 1} = 3.841$$

*Listing of the test  
statistic, degrees of  
freedom, and critical  
value*

Therefore, reject  $H_o$ .

Student survival is contingent upon using the correct answer format when completing Geography 441 exercises ( $\chi^2 = 56.4$ ,  $p < 0.001$ ).

*Statement of the  
results, test statistic,  
and probability*

Research Question: Water temperature and dissolved oxygen measurements were sampled for Burd Run during May of 2003 to determine whether temperature influences dissolved oxygen levels.

*Clearly stated research question.*

$H_0$  : The samples come from a normally distributed population.

$H_A$  : The samples did not come from a normally distributed population..

*Null and alternate hypotheses statements*

$\sigma = 0.05$

*Alpha level*

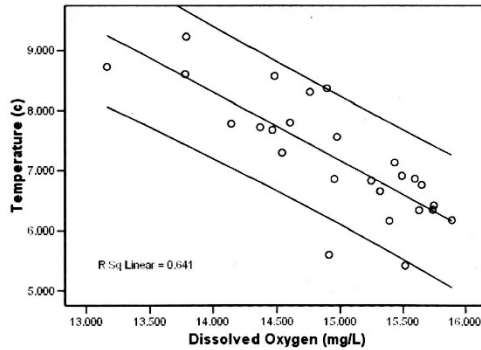
	Tests of Normality					
	Kolmogorov-Smirnov <sup>a</sup>			Shapiro-Wilk		
	Statistic	df	Sig.	Statistic	df	Sig.
Temperature (c)	.126	26	.200*	.974	26	.723
Dissolved Oxygen (mg/L)	.128	26	.200*	.935	26	.104

*Computer results in appropriate order*

\*. This is a lower bound of the true significance.

a. Lilliefors Significance Correction

**Burd Run DO and Temperature  
Measurements: May, 2003**



*Well designed graphic output*

*Note that the manner in which you place you computer output depends on the tests performed*

**Model Summary**

Model	R	R Square	Adjusted R Square	Std. Error of the Estimate
1	.801 <sup>a</sup>	.641	.626	.431070

**ANOVA<sup>b</sup>**

Model		Sum of Squares	df	Mean Square	F	Sig.
1	Regression	7.961	1	7.961	42.845	.000 <sup>a</sup>
	Residual	4.460	24	.186		
	Total	12.421	25			

a. Predictors: (Constant), Temperature (c)

b. Dependent Variable: Dissolved Oxygen (mg/L)

There is a negative linear association between water temperature and dissolved oxygen ( $R^2 = .64$ ,  $p < 0.0001$ ).

*Statement of results, statistic, and probability.*

# **The Scientific Method**

For the record...

The term *data* is plural.

“Collecting *these data* required considerable personal expenditure.”

The scientific method is used because it is *defensible* AND *repeatable*.

- The scientific method is a defensible technique that helps to minimize external influences.
- Statistical analyses are repeatable.
- The scientific method consists of hypotheses, models, laws, and theories.

Hypothesis – a proposition or statement whose truth or falsity is capable of being tested.

Models – a means of simplifying reality so that relationships between variables can be more clearly studied.

Laws – universal statements of unrestricted range.

Theories – a collection of laws that gives greater insight than produced by individual laws; non-speculative.



# **Spatial Data Considerations**

## Spatial Sampling

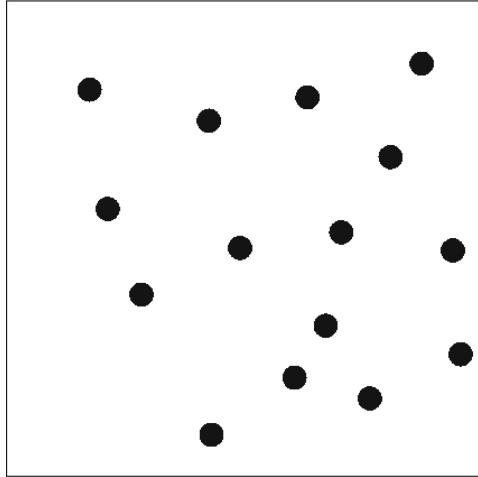
*Sample frame*: the list of all elements within a population.

e.g. All townships within a county.

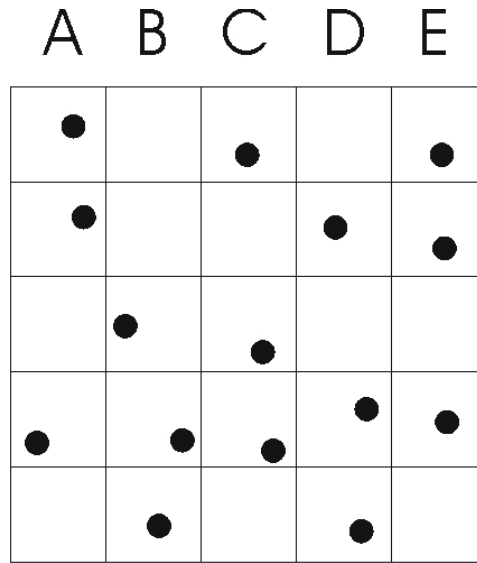
*Sampling method*: the rules which govern how samples of a population are taken.

The three most common are:

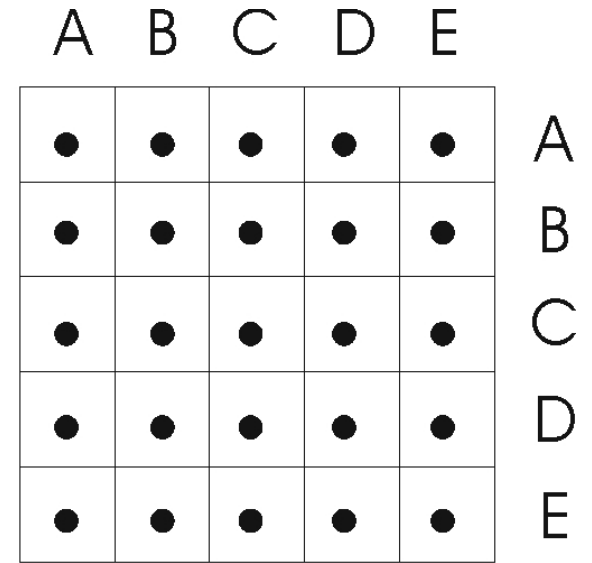
1. Random
2. Stratified random
3. Stratified systematic



**Random**



**Stratified Random**



**Stratified Systematic**

*Random* sampling is often used when it is fairly certain that location does not influence independence.

*Stratified random* sampling is often used when location does influence independence and the degree of influence is known and can be mapped.

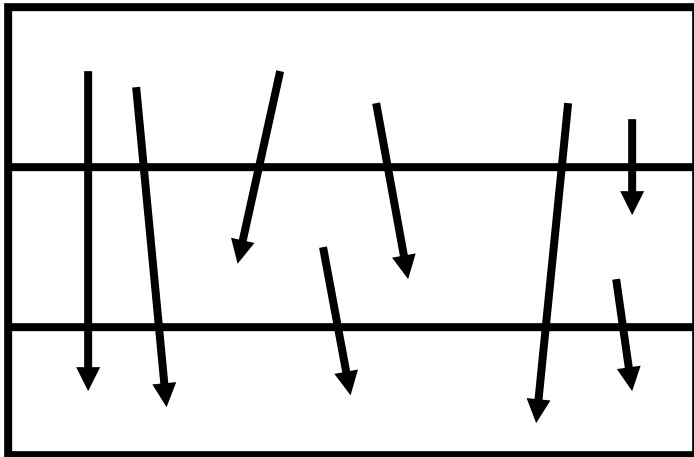
*Stratified systematic* sampling is often used when location does influence independence but the degree of influence is unknown and cannot be mapped.

## Special Considerations with Spatial Data

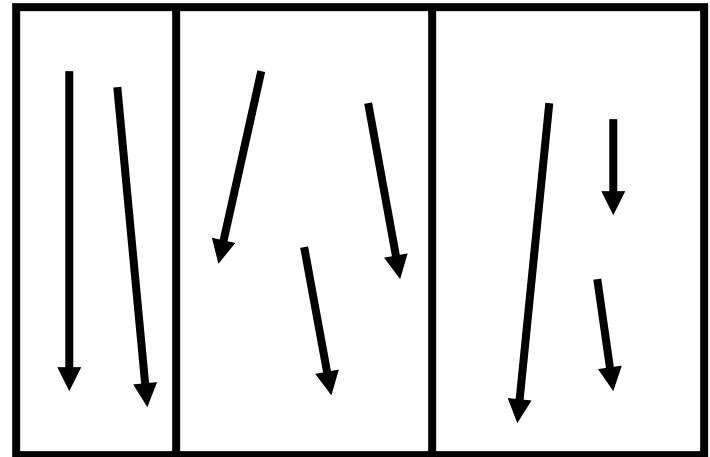
1. Modifiable areal unit problem
2. Boundary problem
3. Spatial sampling procedures
4. Spatial autocorrelation

# 1. Modifiable areal unit problem:

Changes in areal units influence test results.



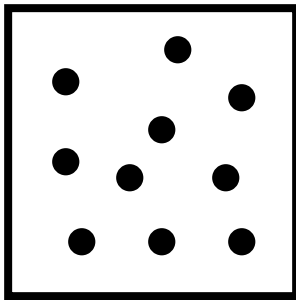
**Cross boundary migration**



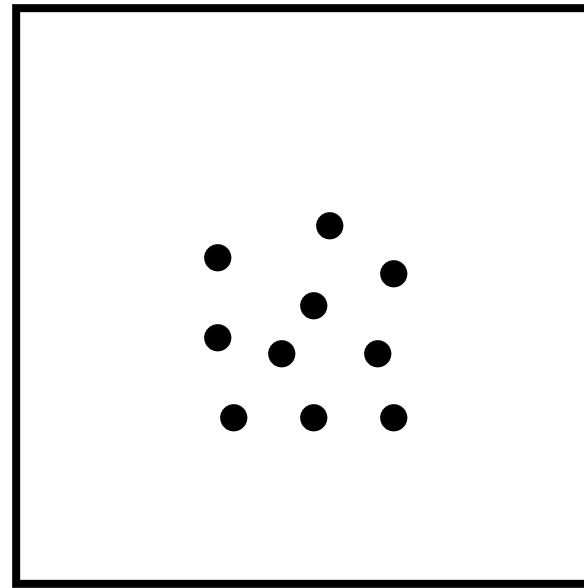
**No cross boundary migration**

## 2. Boundary problem

Changes in the study area boundary influence test results.



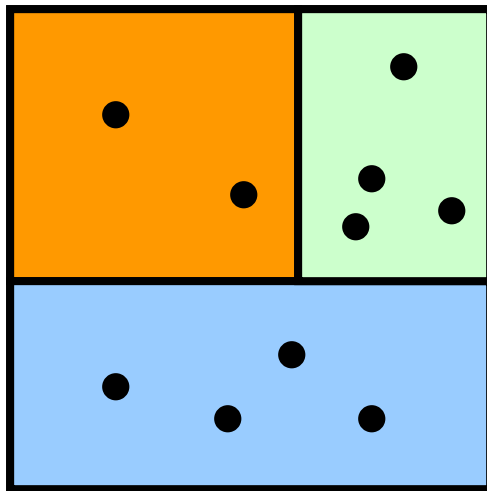
**Small study area,  
even spread of points**



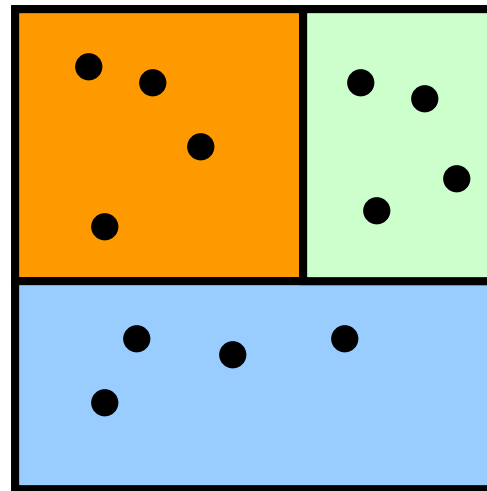
**Large study area,  
clustering of points**

### 3. Spatial sampling procedures

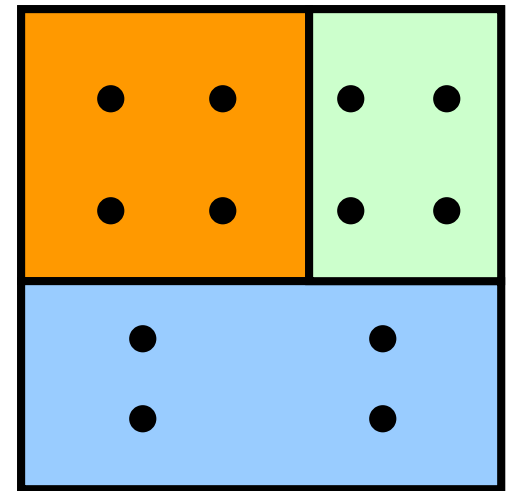
Sampling methods influence test results.



Random



Stratified, Random

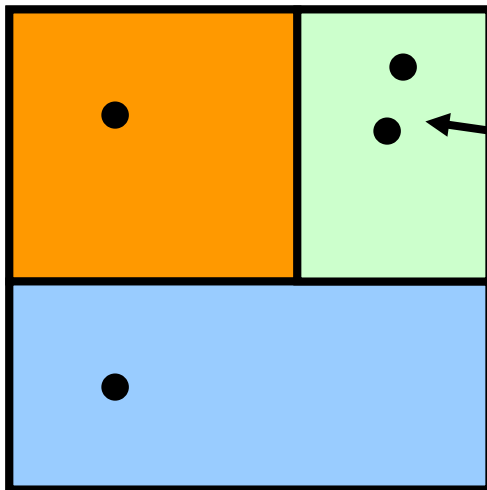


Stratified, Regular



## 4. Spatial autocorrelation

Location near each other often (but not always) influence each other. Non-independence.



These locations have a greater chance of being similar since they are close together.

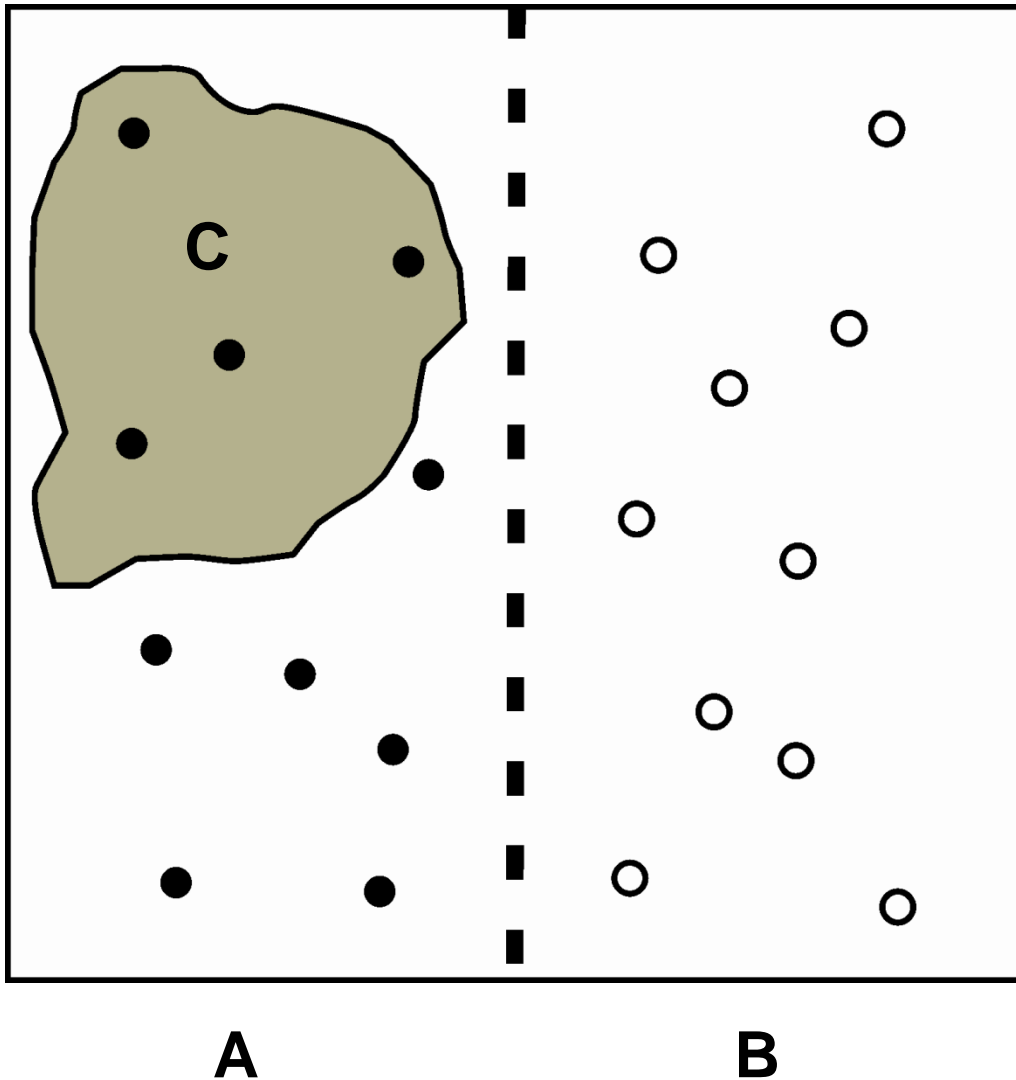
## Spatial Data and Non-independence

- One and two sample tests assume that the data are independent (i.e. one observation does not influence another).
- Unfortunately, with spatial data one observation often *does* influence another.

For example, two ponds near each other may have frogs because they both are located in the correct microclimate.

## Implications of Non-independence

- Non-independence reduces the effective sample size.
- Inflates the degrees of freedom.
- Reduces the critical value.
- Artificially increases the likelihood of getting significant results.



In this example, A and B are study sites. C is a very distinct habitat type.

Habitat C influences the observation values and makes testing between A and B difficult.

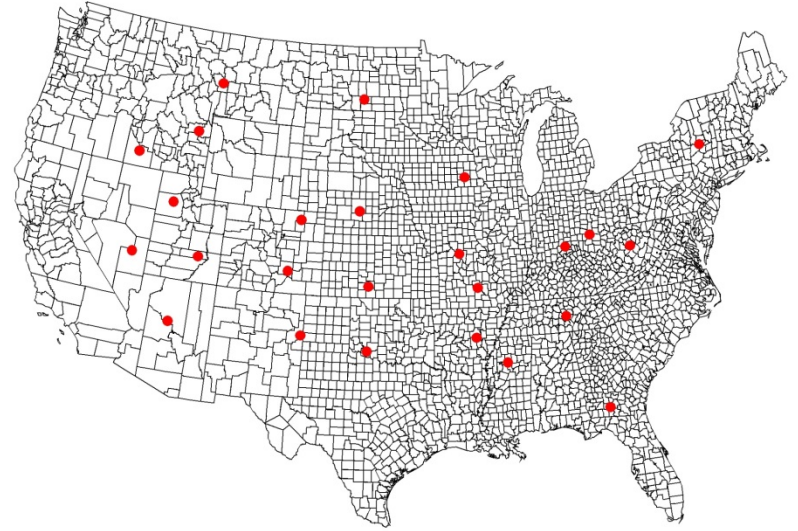
Better to test between A, B, and C.

# Spatial Unit Size and Probability Problem

High probability of any particular state having a dot.



Low probability of any particular county having a dot.



- Probabilities tend to be larger with larger spatial units.
  - The probability that an event will occur is higher with larger spatial units.
  - Small areal units tend to have very low frequencies for random events unless the event is extremely common.
  - Under these conditions a normal distribution is almost impossible to attain.

# Additional Issues with Spatial Data

## 1. Ecological Fallacy

Interpretation errors that occur when results derived from aggregate data are applied to disaggregate data.

- It is something akin to trying to determine someone's grade in a class by looking at the class average.

## 2. The Problem of Scale

Scale only has meaning within the context of the measuring techniques applied and the questions being asked.

- Does it make sense to measure percent forest cover to 5 decimal places? Are we creating “differences” where none actually exist?

### 3. Locational Fallacy

Not all processes have a spatial expression. Certain phenomenon are aspatial.

- For example, burglaries have a spatial component and can be mapped. Embezzlement does not.



## 4. Atomistic Fallacy

An attempt to use individual or disaggregate data to explain aggregate data while ignoring the context of the individuals.

- For example, if we notice that no one is smoking in a bar, then we may conclude that people are smoking less... or it could be a “smoke-free” bar.