Problems - Sections 60, 61, 62

(1) Find the Laurent series that represents the function in the domain $0 < |z| < \infty$.

$$f(z) = z^2 \sin\left(\frac{1}{z^2}\right)$$

(3) Find the Laurent series that represents the function in the domain $1 < |z| < \infty$.

$$f(z) = \frac{1}{1+z}$$

(4) Find two Laurent series that represent the function: one for 0 < |z| < 1 and one for $1 < |z| < \infty$.

$$f(z) = \frac{1}{z^2(1-z)}$$

(5) Find two series that represent the function: the Maclaurin series for |z| < 1 and the Laurent series for $1 < |z| < \infty$.

$$f(z) = \frac{z+1}{z-1}$$