

Problems - Sections 72, 73, 74

(2a) Compute

$$\operatorname{Res}_{-1} \frac{z^{\frac{1}{4}}}{z+1}$$

when the branch cut is at 0.

(2b) Compute

$$\operatorname{Res}_i \frac{\operatorname{Log} z}{(z^2+1)^2}$$

where we are using the principal branch.

(2c) Compute

$$\operatorname{Res}_i \frac{z^{\frac{1}{2}}}{(z^2+1)^2}$$

when the branch cut is at 0.

(3) Evaluate the integral of $f(z) = \frac{3z^3+2}{(z-1)(z^2+9)}$ around the following two contours.

(a) The contour C_a , the circle $|z-2|=2$ positively oriented.

(b) The contour C_b , the circle $|z|=4$ positively oriented.

(4) Evaluate the integral of $\frac{1}{z^3(z+4)}$ around the following two contours.

(a) The contour C_a , $|z|=2$ positively oriented.

(b) The contour C_b , $|z+2|=3$ positively oriented.